

February 16, 2024

References for the lecture  
**Effective Field Theories**

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**Abstract**

This lecture provides an introduction to the framework of low energy effective field theories. After developing the basic concepts, the method is used to analyze electromagnetic, weak and strong interactions at low energies. The course is intended for master or graduate students, who have taken a first course in quantum field theory.

Many of the listed references are freely available through our library and the arXiv preprint server. A useful resource is also the iNSPIRE Hep Database.

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### 2.3 Renormalization group

## 3 Continuum effective theory [3–9]

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### 3.2 Field redefinitions

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### 3.5 Renormalization group improved perturbation theory

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